CONSTELLATION REARRANGEMENT FOR ARQ TRANSMIT DIVERSITY SCHEMES

The present invention relates generally to ARQ (re-) transmission techniques in wireless communication systems and in particular to a method, transceiver and receiver using transmit diversity schemes wherein data packets are transmitted using a first and a second transmission based on a repeat request, and the bit-to-symbol mapping is performed differently for different transmitted diversity branches. The invention is particularly applicable to systems with unreliable and time-varying channel conditions resulting in an improved performance avoiding transmission errors.

There exist several well known transmit diversity techniques wherein one or several redundancy versions relating to identical data are transmitted on several (at least two) diversity branches "by default" without explicitly requesting (by a feedback channel) further diversity branches (as done in an ARQ scheme by requesting retransmissions). For example the following schemes are considered as transmit diversity:

- Site Diversity: The transmitted signal originates from different sites, e.g. different base stations in a cellular environment.

- Antenna Diversity: The transmitted signal originates from different antennas, e.g. different antennas of a multi-antenna base station.

- Polarization Diversity: The transmitted signal is mapped onto different polarizations.

- Frequency Diversity: The transmitted signal is mapped e.g. on different carrier frequencies or on different frequency hopping sequences.

- Time Diversity: The transmitted signal is e.g. mapped on different interleaving sequences.

- Multicode Diversity: The transmitted signal is mapped on different codes in e.g. a CDMA (Code Division Multiple Access) system.

There are known several diversity combining techniques. The following three techniques are the most common ones:

- Selection Combining: Selecting the diversity branch with the highest *SNR*
  for decoding, ignoring the remaining ones.

- Equal Gain Combining: Combining received diversity branches with ignoring
  the differences in received SNR.

- Maximal Ratio Combining: Combining received diversity branches taking the
  received *SNR* of each diversity branch into account.
  The combining can be performed at bit-level (e.g.
  LLR) or at modulation symbol level.

Furthermore, a common technique for error detection/correction is based on Automatic Repeat reQuest (ARQ) schemes together with Forward Error Correction (FEC), called hybrid ARQ (HARQ). If an error is detected within a packet by the Cyclic Redundancy Check (CRC), the receiver requests the transmitter to send additional information (retransmission) to improve the probability to correctly decode the erroneous packet.

In WO-02/067491 A1 a method for hybrid ARQ transmissions has been disclosed which averages the bit reliabilities over successively requested retransmissions by means of signal constellation rearrangement.

As shown therein, when employing higher order modulation formats (e.g. *M*-PSK, *M*-QAM with $\log_2(M) > 2$), where more than 2 bits are mapped onto one modulation symbol, the bits have different reliabilities depending on the chosen mapping. This leads for most FEC (e.g. Turbo Codes) schemes to a degraded decoder performance compared to an input of more equally distributed bit reliabilities.

In conventional communication systems the modulation dependent variations in bit reliabilities are not taken into account and, hence, usually the variations remain after combining the diversity branches at the receiver.

The object of the invention is to provide an ARQ (re-) transmission method, a transmitter and a receiver which show an improved performance with regard to transmission errors. This object is solved by a method, transmitter and receiver as set forth in the independent claims.

The invention is based on the idea to improve the performance at the receiver by applying different signal constellation mappings to the available distinguishable transmit diversity branches and ARQ (re-) transmissions. The invention is applicable

to modulation formats, where more than 2 bits are mapped onto one modulation symbol, since this implies a variation in reliabilities for the bits mapped onto the signal constellation. The variations depend on the employed mapping and on the actually transmitted content of the bits.

Depending on the employed modulation format and the actual number of bits mapped onto a single modulation symbol, for a given arbitrary number (N > 1) of available diversity branches and required retransmissions the quality of the averaging process is different. Averaging in the sense of the present invention is understood as a process of reducing the differences in mean combined bit reliabilities among the different bits of a data symbol. Although it might be that only after using several diversity branches or paths a perfect averaging with no remaining differences is achieved, averaging means in the context of the document any process steps in the direction of reducing the mean combined bit reliability differences. Assuming on average an equal SNR for all available diversity branches and ARQ transmissions, for 16-QAM 4 mappings (4 diversity branches) would be needed to perfectly average out the reliabilities for all bits mapped on any symbol. However, not always the number of available transmit diversity branches and/or the number of ARQ transmissions is sufficient to perform a perfect averaging. Hence, the averaging should then be performed on a best effort basis as shown in the example below.

The present invention will be more readily understood from the following detailed description of preferred embodiments with reference to the accompanying figures which show:

FIG. 1   an example for a 16-QAM signal constellation;

FIG. 2   an example for a different mapping of a 16-QAM signal constellation;

FIG. 3   two further examples of 16-QAM signal constellations;

FIG. 4   an exemplary embodiment of a communication system according to the present invention; and

FIG. 5   details of a table for storing a plurality of signal constellation patterns.

The method described here performs a combined averaging of bit reliabilities considering the transmit diversity branches. The following detailed description is shown for a square 16-QAM with Gray mapping. However, without loss of generality

the shown example is extendable to other M-QAM and M-PSK (with $\log_2(M) > 2$) formats. Moreover, the examples are shown for transmit diversity and HARQ schemes transmitting an identical bit-sequence on both branches and all HARQ transmissions (single redundancy version scheme). Then again, an extension to a transmit diversity and HARQ scheme transmitting only partly identical bits on the diversity branches and HARQ transmissions can be accomplished. An example for a system using multiple redundancy versions is described in copending EP 01127244, filed on November 16, 2001. Assuming a Turbo encoder, the systematic bits can be averaged on a higher level as compared to the parity bits.

Although the below examples give details of an embodiment with the special case of hybrid ARQ (HARQ), it should be noted that the inclusion of an FEC code is not necessary for the present invention to show performance gains. However the highest performance gains can be achieved with the use of HARQ.

The following example describes a method with two diversity branches and HARQ.

1st Transmission:

Assuming a transmit diversity scheme with two generated diversity branches, which are distinguishable at the receiver (e.g. by different spreading or scrambling codes in a CDMA system) and a transmission of the same redundancy version, usually the received diversity branches are combined at the receiver before applying the FEC decoder. A common combining technique is the maximal ratio combining, which can be achieved by adding the calculated log-likelihood-ratios $LLRs$ from each individual received diversity branch.

The log-likelihood-ratio LLR as a soft-metric for the reliability of a demodulated bit b from a received modulation symbol $r = x + jy$ is defined as follows:

$$LLR(b) = \ln\left[\frac{\Pr\{b = 1|r\}}{\Pr\{b = 0|r\}}\right] \qquad (1)$$

As can be seen from Figure 1 (bars indicate rows/columns for which the respective bit equals 1), the mappings of the in-phase component bits and the quadrature component bits on the signal constellation are orthogonal (for M-PSK the LLR calculation cannot be simplified by separating into complex components, however the

general procedure of bit-reliability averaging is similar). Therefore, it is sufficient to focus on the in-phase component bits i_1 and i_2. The same conclusions apply then for q_1 and q_2.

Assuming that Mapping 1 from Figure 1 is applied for the bit-to-symbol mapping for the 1st diversity branch, the log-likelihood-ratio LLR of the most significant bit (MSB) i_1 and the least significant bit (LSB) i_2 yields the following equations for a Gaussian channel:

$$LLR(i_1) = \ln\left[\frac{e^{-K(x+x_0)^2} + e^{-K(x+x_1)^2}}{e^{-K(x-x_0)^2} + e^{-K(x-x_1)^2}}\right] \qquad (2)$$

$$LLR(i_2) = \ln\left[\frac{e^{-K(x-x_1)^2} + e^{-K(x+x_1)^2}}{e^{-K(x-x_0)^2} + e^{-K(x+x_0)^2}}\right] \qquad (3)$$

where x denotes the in-phase component of the normalized received modulation symbol r and K is a factor proportional to the signal-to-noise ratio. Under the assumption of a uniform signal constellation ($x_1 = 3x_0$) equations (2) and (3) can be fairly good approximated approximated, as shown in S. Le Goff, A. Glavieux, C. Berrou, „Turbo-Codes and High Spectral Efficiency Modulation," IEEE SUPERCOMM/ICC '94, Vol. 2 , pp. 645 -649 ,1994, and Ch. Wengerter, A. Golitschek Edler von Elbwart, E. Seidel, G. Velev, M.P. Schmitt, „Advanced Hybrid ARQ Technique Employing a Signal Constellation Rearrangement," IEEE Proceedings of VTC 2002 Fall, Vancouver, Canada, September 2002, by

$$LLR(i_1) \approx -4Kx_0 x \qquad (4)$$

$$LLR(i_2) \approx -4Kx_0\left(2x_0 - |x|\right) \qquad (5)$$

The mean LLR for i_1 and i_2 for a given transmitted modulation symbol yields the values given in Table 1 (substituting $4Kx_0^2$ by Λ). Mean in this sense, refers to that the mean received value for a given transmitted constellation point, exactly matches this transmitted constellation point. Individual samples of course experience noise according to the parameter K. However, for a Gaussian channel the mean value of the noise process is zero. In case of transmitted modulation symbols $0q_1 1q_2$ and

$1q_1 1q_2$, where q_1 and q_2 are arbitrary, the magnitude of the mean LLR (i_1) is higher than of the mean LLR (i_2). This means that the LLR for the MSB i_1 depends on the content of the LSB i_2; e.g. in Figure 1 i_1 has a higher mean reliability in case the logical value for i_2 equals 1 (leftmost and rightmost columns). Hence, assuming a uniform distribution of transmitted modulation symbols, on average 50 % of the MSBs i_1 have about three times the magnitude in LLR of i_2.

Symbol $(i_1 q_1 i_2 q_2)$	Mean value of x	Mean LLR (i_1)	Mean LLR (i_2)
$0q_1 0q_2$	x_0	$-4Kx_0^2 = -\Lambda$	$-4Kx_0^2 = -\Lambda$
$0q_1 1q_2$	x_1	$-12Kx_0^2 = -3\Lambda$	$4Kx_0^2 = \Lambda$
$1q_1 0q_2$	$-x_0$	$4Kx_0^2 = \Lambda$	$-4Kx_0^2 = -\Lambda$
$1q_1 1q_2$	$-x_1$	$12Kx_0^2 = 3\Lambda$	$4Kx_0^2 = \Lambda$

Table 1. Mean LLRs for bits mapped on the in-phase component of the signal constellation for Mapping 1 in Figure 1 according to equations (4) and (5).

If now adding a 2nd transmit diversity branch transmitting e.g. an identical bit sequence prior art schemes would employ an identical mapping to the 1st diversity branch. Here, it is proposed to employ a 2nd signal constellation mapping (Mapping 2) according to Figure 2, which yields the mean LLRs given in Table 2.

Symbol $(i_1 q_1 i_2 q_2)$	Mean value of x	Mean LLR (i_1)	Mean LLR (i_2)
$0q_1 0q_2$	x_0	$-\Lambda$	-3Λ
$0q_1 1q_2$	x_1	$-\Lambda$	3Λ
$1q_1 0q_2$	$-x_0$	Λ	$-\Lambda$
$1q_1 1q_2$	$-x_1$	Λ	Λ

Table 2. Mean LLRs for bits mapped on the in-phase component of the signal constellation for Mapping 2 in Figure 2.

Comparing now the soft-combined LLRs of the received diversity branches applying the constellation rearrangement (Mapping 1+2) and applying the identical mappings (Mapping 1+1, prior art), it can be observed from Table 3 that the combined mean LLR values with applying the constellation rearrangement have a more uniform distribution (Magnitudes: $4 \times 4\Lambda$ and $4 \times 2\Lambda$ instead of $2 \times 6\Lambda$ and $6 \times 2\Lambda$). For most FEC decoders (e.g. Turbo Codes and Convolutional Codes) this leads to a better decoding performance. Investigations have revealed that in particular Turbo

encoding/decoding systems exhibit a superior performance. It should be noted, that the chosen mappings are non exhaustive and more combinations of mappings fulfilling the same requirements can be found.

Transmit Diversity Branch	Symbol $(i_1q_1i_2q_2)$	Constellation Rearrangement (Mapping 1+2)		Prior Art No Rearrangement (Mapping 1+1)	
		Mean $LLR(i_1)$	Mean $LLR(i_2)$	Mean $LLR(i_1)$	Mean $LLR(i_2)$
1	$0q_10q_2$	$-\Lambda$	$-\Lambda$	$-\Lambda$	$-\Lambda$
	$0q_11q_2$	-3Λ	Λ	-3Λ	Λ
	$1q_10q_2$	Λ	$-\Lambda$	Λ	$-\Lambda$
	$1q_11q_2$	3Λ	Λ	3Λ	Λ
2	$0q_10q_2$	$-\Lambda$	-3Λ	$-\Lambda$	$-\Lambda$
	$0q_11q_2$	$-\Lambda$	3Λ	-3Λ	Λ
	$1q_10q_2$	Λ	$-\Lambda$	Λ	$-\Lambda$
	$1q_11q_2$	Λ	Λ	3Λ	Λ
Combined 1+2	$0q_10q_2$	-2Λ	-4Λ	-2Λ	-2Λ
	$0q_11q_2$	-4Λ	-4Λ	-6Λ	2Λ
	$1q_10q_2$	2Λ	-2Λ	2Λ	-2Λ
	$1q_11q_2$	4Λ	2Λ	6Λ	2Λ

Table 3. Mean LLRs (per branch) and combined mean LLRs for bits mapped on the in-phase component of the signal constellation for the diversity branches when employing Mapping 1 and 2 and when employing 2 times Mapping 1.

2nd and further Transmissions:

In case the 1st transmission has not been successfully decoded the receiver requests a retransmission (2nd transmission). Assuming for 2nd transmission also 2 transmit diversity branches are available, the 2 additional mappings (mapping 3 and mapping 4 in Figure 3) are employed to further improve the averaging of the bit reliabilities as shown in Table 4. In this example (assuming an equal SNR for all received signals) the averaging is performed perfectly after receiving 2 transmit diversity branches times 2 transmissions (possibility to employ 4 different mappings – sufficient for 16-QAM). Table 4 compares the LLRs with and without applying the proposed Constellation Rearrangement. Having a closer look at the combined LLRs, it can be seen that with application of the Constellation Rearrangement the magnitude for all bit reliabilities results in 6Λ.

It should be noted again, that the chosen mappings are non exhaustive and more combinations of mappings fulfilling the same requirements can be found.

Transmit Diversity Branch	Transmission Number	Symbol ($i_1q_1i_2q_2$)	Constellation Rearrangement (Mapping 1+2+3+4)		Prior Art No Rearrangement (Mapping 1+1+1+1)	
			Mean LLR (i_1)	Mean LLR (i_2)	Mean LLR (i_1)	Mean LLR (i_2)
1	1	$0q_10q_2$	$-\Lambda$	$-\Lambda$	$-\Lambda$	$-\Lambda$
		$0q_11q_2$	-3Λ	Λ	-3Λ	Λ
		$1q_10q_2$	Λ	$-\Lambda$	Λ	$-\Lambda$
		$1q_11q_2$	3Λ	Λ	3Λ	Λ
2	1	$0q_10q_2$	$-\Lambda$	-3Λ	$-\Lambda$	$-\Lambda$
		$0q_11q_2$	$-\Lambda$	3Λ	-3Λ	Λ
		$1q_10q_2$	Λ	$-\Lambda$	Λ	$-\Lambda$
		$1q_11q_2$	Λ	Λ	3Λ	Λ
3	2	$0q_10q_2$	$-\Lambda$	$-\Lambda$	$-\Lambda$	$-\Lambda$
		$0q_11q_2$	$-\Lambda$	Λ	-3Λ	Λ
		$1q_10q_2$	Λ	-3Λ	Λ	$-\Lambda$
		$1q_11q_2$	Λ	3Λ	3Λ	Λ
4	2	$0q_10q_2$	-3Λ	$-\Lambda$	$-\Lambda$	$-\Lambda$
		$0q_11q_2$	$-\Lambda$	Λ	-3Λ	Λ
		$1q_10q_2$	3Λ	$-\Lambda$	Λ	$-\Lambda$
		$1q_11q_2$	Λ	Λ	3Λ	Λ
Combined 1+2+3+4		$0q_10q_2$	-6Λ	-6Λ	-4Λ	-4Λ
		$0q_11q_2$	-6Λ	6Λ	-12Λ	4Λ
		$1q_10q_2$	6Λ	-6Λ	4Λ	-4Λ
		$1q_11q_2$	6Λ	6Λ	12Λ	4Λ

Table 4. Mean *LLR*s (per branch) and combined mean *LLR*s for bits mapped on the in-phase component of the signal constellation for the diversity branches and (re-) transmissions when employing Mappings 1 to 4 and when employing 4 times Mapping 1.

If the constellation rearrangement is performed by applying different mapping schemes, one would end up in employing a number of different mappings as given in Figure 1, Figure 2 and Figure 3. If the identical mapper (e.g. Figure 1) should be kept for all transmit diversity branches, e.g. mapping 2 can be obtained from mapping 1 by the following operations:

- exchange positions of original bits i_1 and i_2
- exchange positions of original bits q_1 and q_2

- logical bit inversion of original bits i_1 and q_1

Alternatively, those bits that end in positions 1 and 2 can also be inverted (resulting in a different mapping with an identical bit-reliability characteristics).

Therefore, the following table provides an example how to obtain mappings 1 to 4 (or mappings with equivalent bit reliabilities for i_1, i_2, q_1 and q_2), where the bits always refer to the first transmission, and a long dash above a character denotes logical bit inversion of that bit:

Mapping No.	Interleaver and Inverter functionality
1	$i_1 q_1 i_2 q_2$
2	$\overline{i_2}\,\overline{q_2}\,\overline{i_1}\,\overline{q_1}$ or $i_2 q_2 \overline{i_1}\,\overline{q_1}$
3	$\overline{i_2}\,\overline{q_2}\,i_1 q_1$ or $i_2 q_2 i_1 q_1$
4	$i_1 q_1 \overline{i_2}\,\overline{q_2}$ or $\overline{i_1}\,\overline{q_1}\,\overline{i_2}\,\overline{q_2}$

Table 5. Alternative implementation of the Constellation Rearrangement by interleaving (intra-symbol interleaving) and logical inversion of bits mapped onto the modulation symbols.

Generally at least 2 different mappings should be employed for $N > 1$ diversity branches, where the order and the selection of the mappings is irrelevant, as long as the bit-reliability averaging process, meaning the reduction in differences in bit reliabilities) is maintained.

Preferred realizations in terms of number of employed mappings

- o M-QAM
  - Employing $\log_2(M)$ different mappings
  - Employing $\log_2(M)/2$ different mappings
- o M-PSK
  - Employing $\log_2(M)$ different mappings
  - Employing $\log_2(M)/2$ different mappings
  - Employing $2\log_2(M)$ different mappings

The applied signal constellation mappings for modulation at the transmitter and demodulation at the receiver need to match for each individual transmit diversity

branch. This can be achieved by appropriate signalling of parameters indicating the proper mapping or combination of mappings to be applied for the diversity branches and HARQ transmissions. Alternatively the definition of the mappings to be applied for transmit diversity branches and HARQ transmissions may be system predefined.

Figure 4 shows an exemplary embodiment of a communication system according to the present invention. More specifically, the communication system comprises a transmitter 10 and a receiver 20 which communicate through a communication channel consisting of a plurality of diversity branches 40A, 40B and 40C. Although three diversity branches are illustrated in the figure, it becomes clear to a person skilled in the art that an arbitrary number of branches may be chosen. From a data source 11, data packets are supplied to a FEC encoder 12, preferably a FEC Turbo encoder, where redundancy bits are added to correct errors. The bits output from the FEC encoder are subsequently supplied to a mapping unit 13 acting as a modulator to output symbols formed according to the applied modulation scheme stored as a constellation pattern in a table 15. Subsequently the data symbols are applied to a transmission unit 30 for transmission over the branches 40A – C. The receiver 20 receives the data packets by the receiving unit 35. The bits are then input into a demapping unit 21 which acts as a demodulator using the same signal constellation pattern stored in the table 15 which was used during the modulation of these bits.

The demodulated data packets received over one diversity branch are stored in a temporary buffer 22 for subsequent combining in a combining unit 23 with the data packets received over at least one other diversity branch.

A retransmission is launched by an automatic repeat request issued by an error detector (not shown) with the result that an identical data packet is transmitted from the transmitter 10. In the combining unit 23, the previously received erroneous data packets are soft-combined with the retransmitted data packets. Then a decoder decodes the bits and output a measure for the transmission quality, e.g. the bit-error-rate BER.

As illustrated in figure 5, table 15 stores a plurality of signal constellation patterns #0..#n which are selected for the individual transmissions over the individual diversity

branches and HARQ transmissions according to a predetermined scheme. The scheme, i.e. the sequence of signal constellation patterns used for modulating/-demodulating are either pre-stored in the transmitter and the receiver or are signalled by transmitter to the receiver prior to usage.